



Software Engineering and Architecture

Systematic Testing
Equivalence Class Partitioning

What is reliability?

Definition: Reliability (ISO 9126)

The capability of the software product to maintain a specified level of performance when used under specified conditions.

- If there is a defect, it may fail and is thus not reliable.
- Thus:
 - Reduce number of defects
 - ... will reduce number of failures
 - ... will increase reliability

Discussion

- True?
 - Find example of **removing a defect does not increase the system's reliability at all**
 - Find example of **removing defect 1 increase reliability dramatically while removing defect 2 does not**



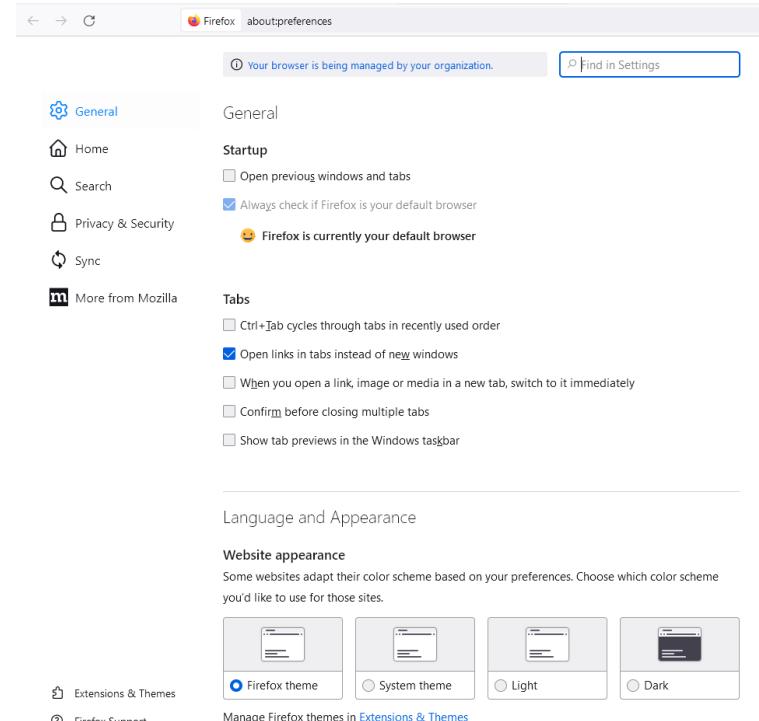
All defects are not equal!

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- So – given a certain amount of time to find defects (you need to sell things to earn money!):
- What kind of defects should you correct to get best *return on investment*?

Example

- Firefox has an enormous amount of possible configurations! Imagine testing *all possible combinations!*
- Which one would you test most thoroughly?





Testing Techniques

One viewpoint

- The probability of defects is a function of the code *complexity*. Thus we may identify (at least) three different testing approaches:
 - **No testing.** Complexity is so low that the test code will become more complex or longer. Example: set/get methods
 - **Explorative** testing: “gut feeling”, experience. TDD relies heavily on ‘making the smart test case’ but does not dictate any method.

Definition: **Systematic testing**

Systematic testing is a planned and systematic process with the explicit goal of finding defects in some well-defined part of the system.

Destructive!

- Testing is a *destructive process!!!*
 - In contrast to almost all other SW processes which are constructive!
- Human psychology
 - **I want to be a success**
 - **The brain will deliver!**
 - (ok, X-factor shows this is not always the case...)
- *I will prove my software works*
- *I will prove my software is really lousy*

- When testing, reprogram your brains

• ***I am a success if I find a defect.
The more I find, the better I am!***

- There are a *lot* of different testing techniques.
- Types:

Definition: **Black-box testing**

The *unit under test* (UUT) is treated as a black box. The only knowledge we have to guide our testing effort is the specification of the UUT and a general knowledge of common programming techniques, algorithmic constructs, and common mistakes made by programmers.

Definition: **White-box testing**

The full implementation of the unit under test is known, so the actual code can be inspected in order to generate test cases.

- In our course – two **black box** techniques:
 - Equivalence class partitioning (EC)
 - Boundary value analysis (which is actually associated with EC)



Equivalence Class Partitioning

Often just called EC testing...

- `Math.abs(x)`: Absolute value of x ;
 - Examples: $\text{abs}(-2) = 2$; $\text{abs}(7) = 7$;
 - If x is not negative, return x .
 - If x is negative, return the negation of x .
- Will these five test cases ensure a reliable implementation?

Unit under test: <code>Math.abs</code>	
Input	Expected output
$x = 37$	37
$x = 38$	38
$x = 39$	39
$x = 40$	40
$x = 41$	41

Two problems

- A) what is the probability that $x=38$ will find a defect that $x=37$ did not expose?
- B) what is the probability that there will be a defect in handling negative x ?

Unit under test: Math.abs	
Input	Expected output
$x = 37$	37
$x = 38$	38
$x = 39$	39
$x = 40$	40
$x = 41$	41

```
public static int abs(int x) { return x; }
```

- *We can find a **single** input value that represents a **large set of values** when it comes to finding defects!*

Definition: Equivalence class (EC)

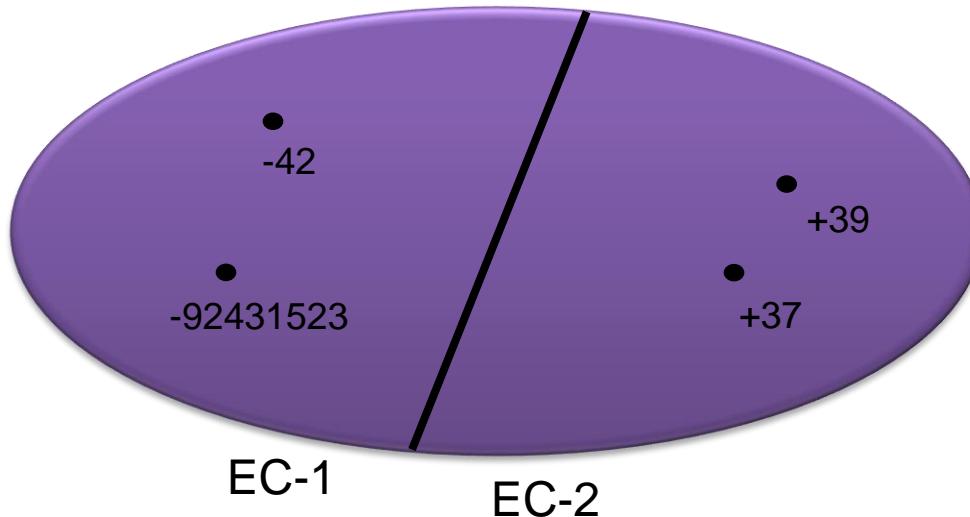
A subset of all possible inputs to the UUT that has the property that if one element in the subset demonstrates a defect during testing, then we assume that all other elements in the subset will demonstrate the *same* defect.

An EC is a (sub)set of all inputs.

Da: Delmængde

- So – we *only need one test case representing that set*

- ECs are subsets of the *full input set*.



Unit under test: Math.abs	
Input	Expected output
$x = 37$	37
$x = 38$	38
$x = 39$	39
$x = 40$	40
$x = 41$	41
$x = -42$	42

The argumentation

- The specification will force an implementation where (most likely!) all *positive* arguments are treated by one code fragment and all *negative* arguments by another.
 - Thus we *only need two test cases*:
 - 1) one that tests the positive argument handling code
 - 2) one that tests the negative argument handling code
- For 1) $x=37$ is just as good as $x=1232$, etc. Thus we simply *select a representative element* from each EC and generate a test case based upon it.

- Systematic testing ...
- **does not mean**
 - *Systematically find all defects and guaranty none are left!!!*
 - *If you need proofs, you need my colleagues research ☺*
- **does mean**
 - Systematically derive a *small set of test cases with high probability of finding many defects!!!*



Specifically

- Systematic testing cannot in any way counter *malicious programming*
 - *Virus, easter eggs, evil-minded programmers*
 - *(really really incompetent programmers)*

A Sound EC partitioning

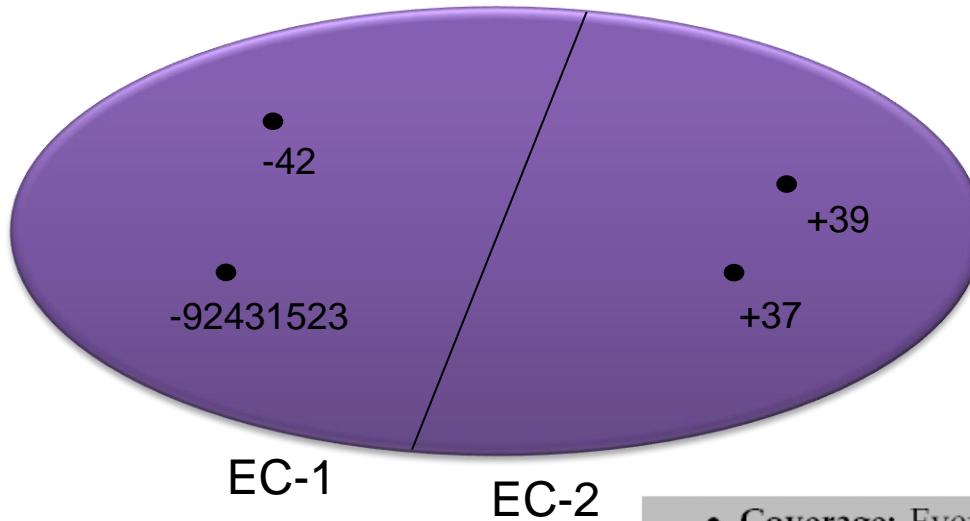
- For our ECs to be *sound*:

- **Coverage:** Every possible input element belongs to at least one of the equivalence classes.
- **Representation:** If a defect is demonstrated on a particular member of an equivalence class, the same defect is assumed to be demonstrated by any other member of the class.

- *Exercise*

- *Why the word ‘assumed’ in the above statement?*
 - *Why not ‘guaranteed’?*

- Coverage? Representation?



- **Coverage:** Every possible input element belongs to at least one of the equivalence classes.
- **Representation:** If a defect is demonstrated on a particular member of an equivalence class, the same defect is assumed to be demonstrated by any other member of the class.

- The classic blunder at exams!
 - *Representation = two values from the same EC will result in the same behaviour in the algorithm*
- Argue why this is completely wrong!
 - Consider for instance the Account class' deposit method...
 - `account.deposit(100);`
 - `account.deposit(1000000);`

- Open.kattis // Exercise **International Dates**

DATE	PROBLEM	JUDGEMENT	RUNTIME	LANGUAGE	TEST CASES
20:05:30	International Dates	Accepted	0.09 s	Java	109/109



- *109 test cases for five lines of code???*
- My analysis:
 - **3 test cases is enough!**

EC Covered	TestCase	Expected
[o1][f2][s1]	13/07/1963	EU
[o2][f1][s2]	08/13/2027	US
[o3][f1][s1]	12/12/1987	either

```
public static String classifyFormat(String dateString) {  
    String parts[] = dateString.split( regex: "/" );  
    int p1 = Integer.parseInt(parts[0]);  
    int p2 = Integer.parseInt(parts[1]);  
    // US MM/DD - bail out if DD > 12  
    if (p2 > 12) return "US";  
    // EU DD/MM - bail out if DD > 12  
    if (p1 > 12) return "EU";  
    return "either";  
}
```

Documenting ECs

- Math.abs is simple. Thus the ECs are simple.
- This is often **not** the case! Finding ECs requires deep thinking, analysis, and iteration.
- Document them!
- **Equivalence class table:**

Label the EC

Condition	Invalid ECs	Valid ECs
absolute value of x	-	$x > 0[a1]$ $x \leq 0[a2]$

Invalid/Valid ECs

- Some input values make an algorithm *give up, bail out, throw exception, or compute answer immediately*:
 - `file.open("nonexistingfile");`
 - `game.usePower(FINDUS)` (and findus mana =0)
- Input values that leads to *abnormal processing/bail out*, we classify as belonging to ***invalid ECs***.
- Those input values that process normally/all the way, we say belong to ***valid ECs***.
 - Those cases where the ‘method is run to conclusion’

Bail out fast

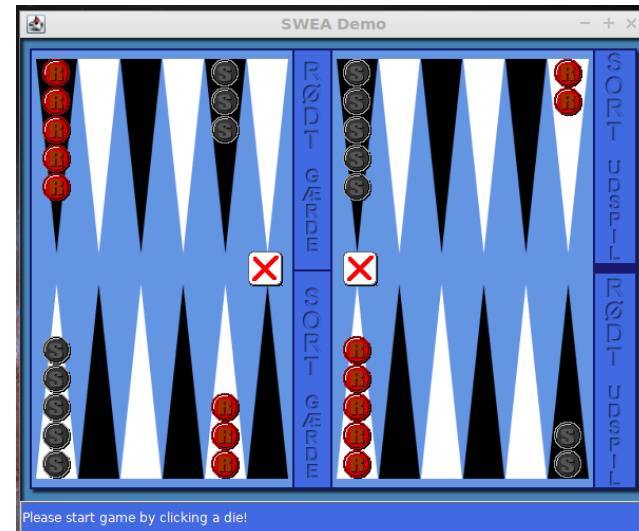


Finding the ECs

Often tricky...

Example: Backgammon move validation

- **validity = v (move, player, board-state, die-value)**
 - is Red move (B1-B2) valid on this board given these die values and this player in turn?
- Problem:
 - multiple parameters: player, move, board, die
 - complex parameters: board state
 - coupled parameters: die couples to move!
 - EC boundary is not a constant!



A process

- To find the ECs you will need to look carefully at the specification and especially all the **conditions** associated.
 - Conditions express choices in our algorithms and therefore typically defines disjoint algorithm parts!
 - **If (expr) {} else {}**
 - And as the test cases should at least run through all parts of the algorithms, it defines the boundaries for the ECs.
- ... And consider typical programming techniques
 - Will a program contain if's and while's here?

Partitioning Heuristics

- 1) If you have a *range of values* specification
 - make **three** ECs:

• [1] in range	valid
• [2] above range	invalid
• [3] below range	invalid
- Ex. Standard chess notation/ is “a8” or “x17” valid positions?
 - **Column range: a-h; Row range: 1-8**

Condition	Invalid ECs	Valid ECs
Column	$< 'a' [a1]; > 'h' [a2]$	$'a'-'h' [a3]$
Row	$< 1 [b1]; > 8 [b2]$	$1-8 [b3]$

Chess Board Numbers



Black sets up on the top

Chess board square notation

From left-to-right from White's perspective, the squares are ordered alphabetically with letters from "a" through to "h".

Each square also gets a unique number, from "1" to "8". The rank closest to the White player in the initial setup are "1" squares, the next rank the "2" squares and so on... to the rank closest to Black, which are "8" squares.

White will set up on the bottom of the board

Partitioning Heuristics

- 2) If you have a set, S , of values specification
 - make $|S|+1$ ECs
 - $[1] \dots [|S|]$ one EC for each member in S valid
 - Each with only that particular member in the set
 - $[|S|+1]$ for a value outside S invalid
- Ex. PayStation accepting coins
 - Set of $\{5, 10, 25\}$ cents coins

Condition	Invalid ECs	Valid ECs
Allowed coins	$\notin \{5, 10, 25\}$ [a1]	$\{5\}$ [a2]; $\{10\}$ [a3]; $\{25\}$ [a4]

- Note: Not just *two sets!*

Partitioning Heuristics

- 3) If you have a *boolean condition* specification
 - make **two** ECs
- Ex. the first character of identifier must be a letter

Condition	Invalid ECs	Valid ECs
Initial character of identifier	non-letter [a1]	letter [a2]

- the object reference must not be null
 - *you get it, right?* ☺



Partitioning Heuristics

- 4) If you question the representation property of any EC, then repartition!
 - Split EC into smaller ECs
- Examples: shortly ☺



From ECs to Test cases

Test case generation

- For disjoint ECs you simply pick an element from each EC to make a test case.
- Document in a **Extended test case table**

ECs covered	Test case	Expected output
$[a1]$	$x = 201$	$+201$
$[a2]$	$x = -87$	$+87$

- Augmented with a column showing which ECs are covered!

Condition	Invalid ECs	Valid ECs
absolute value of x	–	$x > 0[a1]$ $x \leq 0[a2]$

Usual case

- ECs are seldom disjoint – so you have to *combine* them to generate test cases.
- Ex. Chess board validation

Condition	Invalid ECs	Valid ECs
Column	< 'a' [a1]; > 'h' [a2]	'a'–'h' [a3]
Row	< 1 [b1]; > 8 [b2]	1–8 [b3]

ECs covered	Test case	Expected output
[a1], [b1]	(' ', 0)	illegal
[a2], [b1]	('i', -2)	illegal
[a3], [b1]	('e', 0)	illegal
[a1], [b2]	(' ', 9)	illegal
[a2], [b2]	('j', 9)	illegal
[a3], [b2]	('f', 12)	illegal
[a1], [b3]	(' ', 4)	illegal
[a2], [b3]	('i', 5)	illegal
[a3], [b3]	('b', 6)	legal

Combinatorial Explosion

- Umph! Combinatorial explosion of test cases 😞.
- Ex.
 - **Three** independent input parameters $\text{foo}(x,y,z)$
 - **Four** ECs for each parameter
 - That is:
 - x's input set divided into four ECs,
 - y's input set divided into four ECs,
 - etc.
- Question:
 - How many test cases?



Combinatorial Explosion

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- Answer: $4^3 = 64$ test cases...
- TC1: [ECx1],[ECy1],[ECz1]
- TC2: [ECx1],[ECy1],[ECz2] ...
- TC4: [ECx1],[ECy1],[ECz4] ...
- TC5: [ECx1],[ECy2],[ECz1] ...
- TC9: [ECx1],[ECy3],[ECz1] ...
- ...
- TC64: [ECx4],[ECy4],[ECz4]

Myers' Heuristics

- Often, it is better to generate test cases like this:

- Until all valid ECs have been covered, define a test case that covers as many uncovered valid ECs as possible.
- Until all invalid ECs have been covered, define a test case whose element only lies in a single invalid ECs.

Condition	Invalid ECs	Valid ECs
Column	< 'a' [a1]; > 'h' [a2]	'a'-'h' [a3]
Row	< 1 [b1]; > 8 [b2]	1-8 [b3]

ECs covered	Test case	Expected output
[a1], [b3]	(' ',5)	illegal
[a2], [b3]	('j',3)	illegal
[a3], [b1]	('b',0)	illegal
[a3], [b2]	('c',9)	illegal
[a3], [b3]	('b',6)	legal

Rule 2

Rule 1

Why Rule 2?

- Due to **masking**
 - One correct test *masks* a later incorrect test
- Ex.

```
public class ChessBoard {  
    public boolean valid(char column, int row) {  
        if ( column < 'a' ) { return false; }  
        if ( row < 0 ) { return false; }  
        return true;  
    }  
}
```

```
assertThat(b.valid(' ',0)), is(false));
```

False positive

- Test case (' ',0) will pass which is expected
 - Code deemed correct, but this is a **wrong** conclusion!
 - It was the 'column' test that returned 'false' so the defect in the row conditions is **masked**

Why Rule 1?

- You may combine as *many* valid ECs as possible and cover it with only a single test case until all valid ECs are exhausted...
- Why?
- Because I must assume that all elements from ECs are used to compute the final result. Any defects will thus most likely show up even if the defect only relate to one element.
- Ex. `bankdayNumberInYear(int month, int day)`
 - return $30 * \text{month} + \text{day}$

Jan = 1; Feb = 2



The Process

The Summary

1. Review the requirements for the UUT and identify *conditions* and use the heuristics to find ECs for each condition. ECs are best written down in an *equivalence class table*.
2. Review the produced ECs and consider carefully the representation property of elements in each EC. If you question if particular elements are really representative then repartition the EC.
3. Review to verify that the coverage property is fulfilled.
4. Generate test cases from the ECs. You can often use Myers heuristics for combination to generate a minimal set of test cases. Test cases are best documented using a *test case table*.
5. **Review the generated test cases carefully to find what you missed – and iterate!**



An Example

Phew – let's see things in practice

Example

```
public interface weekday {  
  
    /** calculate the weekday of the 1st day of the given month.  
     * @param year the year as integer. 2000 means year 2000 etc. Only  
     * years in the range 1900-3000 are valid. The output is undefined  
     * for years outside this range.  
     * @param month the month as integer. 1 means January, 12 means  
     * December. Values outside the range 1-12 are illegal.  
     * @return the weekday of the 1st day of the month. 0 means Sunday,  
     * 1 means Monday etc. up til 6 meaning Saturday.  
    */  
    public int weekday(int year, int month)  
        throws IllegalArgumentException;  
}
```

- Which heuristics to use on the spec?
- **Range:** *If a condition is specified as a range of values*, select one valid EC that covers the allowed range, and two invalid ECs, one above and one below the end of the range.
- **Set:** *If a condition is specified as a set of values* then define an EC for each value in the set and one EC containing all elements outside the set.
- **Boolean:** *If a condition is specified as a “must be” condition* then define one EC for the condition being true and one EC for the condition being false.

Process step 1

- Result

Condition	Invalid ECs	Valid ECs
year	$< 1900 [y1]; > 3000 [y2]$	$1900 - 3000 [y3]$
month	$< 1 [m1]; > 12 [m2]$	$1 - 12 [m3]$

Process step 2

- Review and consider representation property?

Condition	Invalid ECs	Valid ECs
year	$< 1900 [y1]; > 3000 [y2]$	$1900 - 3000 [y3]$
month	$< 1 [m1]; > 12 [m2]$	$1 - 12 [m3]$

Damn – Leap years!

- Nice to be an astronomer ☺

Condition	Invalid ECs	Valid ECs
year (y)		$\{y \mid y \in [1900; 3000] \wedge y \% 400 = 0\}$ [y3a] $\{y \mid y \in [1900; 3000] \wedge y \% 100 = 0 \wedge y \notin [y3a]\}$ [y3b] $\{y \mid y \in [1900; 3000] \wedge y \% 4 = 0 \wedge y \notin [y3a] \cup [y3b]\}$ [y3c] $\{y \mid y \in [1900; 3000] \wedge y \% 4 \neq 0\}$ [y3d]

- What about the months? Let's play it safe...

Condition	Invalid ECs	Valid ECs
month		1 – 2 [m3a]; 3 – 12 [m3b]

Process step 3

- Coverage?

Condition	Invalid ECs	Valid ECs
year (y)		$\{y \mid y \in [1900; 3000] \wedge y \% 400 = 0\}$ [y3a] $\{y \mid y \in [1900; 3000] \wedge y \% 100 = 0 \wedge y \notin [y3a]\}$ [y3b] $\{y \mid y \in [1900; 3000] \wedge y \% 4 = 0 \wedge y \notin [y3a] \cup [y3b]\}$ [y3c] $\{y \mid y \in [1900; 3000] \wedge y \% 4 \neq 0\}$ [y3d]

Condition	Invalid ECs	Valid ECs
month		1 – 2 [m3a]; 3 – 12 [m3b]

Process step 4

- Generate, using Myers rule 1 and rule 2

ECs covered	Test case	Expected	Condition	Invalid ECs	Valid ECs
$[y3a], [m3a]$	$y = 2000; m = 2$		year (y)		$\{y y \in [1900; 3000] \wedge y \% 400 = 0\} [y3a]$
$[y3b], [m3b]$	$y = 1900; m = 5$				$\{y y \in [1900; 3000] \wedge y \% 100 = 0 \wedge y \notin [y3a]\} [y3b]$
$[y3c], [m3b]$	$y = 2004; m = 10$				$\{y y \in [1900; 3000] \wedge y \% 4 = 0 \wedge y \notin [y3a] \cup [y3b]\} [y3c]$
$[y3d], [m3a]$	$y = 1985; m = 1$				$\{y y \in [1900; 3000] \wedge y \% 4 \neq 0\} [y3d]$
$[y1], [m3b]$	$y = 1844; m = 4$	[exception]	5		
$[y2], [m3b]$	$y = 4231; m = 8$	[exception]	-	month	$1 - 2 [m3a]; 3 - 12 [m3b]$
$[m1], [y3d]$	$y = 2003; m = 0$	[exception]			
$[m2], [y3c]$	$y = 2004; m = 13$	[exception]			

- Conclusion: Only 8 test cases for a rather tricky alg.



Example 2

Formatting

```
/** format a string representing of a double. The string is always
6 characters wide and in the form ###.##, that is the double is
rounded to 2 digit precision. Numbers smaller than 100 have '0'
prefix. Example: 123 -> '123.00'; 2,3476 -> '002.35' etc. If the
number is larger or equal to 999.995 then '*****' is output to
signal overflow. All negative values are signaled with '---.---'
*/
public String format(double x);
```

- Note! Most of the conditions do **not** really talk about x but on the output.
- Remember: *Conditions in the specs!!!*

- What do we do?

```
/** format a string representing of a double. The string is always
   6 characters wide and in the form ###.##, that is the double is
   rounded to 2 digit precision. Numbers smaller than 100 have '0'
   prefix. Example: 123 -> '123.00'; 2,3476 -> '002.35' etc. If the
   number is larger or equal to 999.995 then '*****' is output to
   signal overflow. All negative values are signaled with '---.---'
*/
public String format(double x);
```

- Range? Boolean? Set?
- Valid / Invalid ECs?

My analysis

Condition	Invalid ECs	Valid ECs	
overflow / underflow	$\geq 1000.0 [a1]; < 0.0 [a2]$	$0.0 \leq x < 1000.0 [a3]$	range
2 digit rounding		(,00x round up) [b1]; (,00x round down) [b2]	boolean
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]	set
output suffix		'.yx' suffix ($x \neq 0$)[d1] '.x0' suffix ($x \neq 0$)[d2] exact '.00' suffix [d3]	set

Test cases

ECs covered	Test case	Expected output
[a1]	1234.456	'***.*'
[a2]	-0.1	'__._'
[b1], [c1], [d1]	212.738	'212.74'
[b2], [c2], [d2]	32.503	'032.50'
[b1], [c3], [d3]	7.995	'008.00'
[b2], [c4], [d1]	0.933	'000.93'

Condition	Invalid ECs	Valid ECs
overflow / underflow	≥ 1000.0 [a1]; < 0.0 [a2]	
2 digit rounding		(,00x round up) [b1]; (,00x round down) [b2]
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
output suffix		'.yx' suffix ($x \neq 0$)[d1] .x0' suffix ($x \neq 0$)[d2] exact '.00' suffix [d3]

Process Recap

1. Until all valid ECs have been covered, define a test case that covers as many uncovered valid ECs as possible.

Condition	Invalid ECs	Valid
overflow / underflow	≥ 1000.0 [a1]	(,00x round up) [b1]
2 digit rounding	< 0.0 [a2]	(,00x round down) [b2]
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
output suffix		'.yx' suffix ($y \neq 0$) [d1] '.x0' suffix ($x \neq 0$) [d2] exact '.00' suffix [d3]

2. Until all invalid ECs have been covered, define a test case whose elements lies in a single invalid ECs.

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overflow / underflow	≥ 1000.0 [a1]; < 0.0 [a2]	(,00x round 00x round down) [b2]
2 digit rounding		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
prefix		'.yx' suffix ($x \neq 0$) [d1] '.x0' suffix ($x \neq 0$) [d2]
output suffix		exact '.00' suffix [d3]

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2 digit rounding		(,00x round up) [b1]; (,00x round down) [b2]
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
output suffix		'.yx' suffix ($x \neq 0$) [d1] .x0' suffix ($x \neq 0$) [d2] exact '.00' suffix [d3]

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2 digit rounding		(,00x round up) [b1]; (,00x round down) [b2]
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
output suffix		'.yx' suffix ($x \neq 0$) [d1] .x0' suffix ($x \neq 0$) [d2] exact '.00' suffix [d3]

ECs covered	Test case	Expected output
[a1]	1234.456	'***.***'
[a2]	-0.1	'__._'
[a1], [c1], [d1]	212.738	'212.74'
[b2], [c2], [d2]	32.503	'032.50'
[b1], [c3], [d3]	7.995	'008.00'
[b2], [c4], [d1]	0.933	'000.93'

Process Recap

1. Until all valid ECs have been covered, define a test case that covers as many uncovered valid ECs as possible.
2. Until all invalid ECs have been covered, define a test case whose elements lies in a single invalid ECs.

Condition	Invalid ECs	Valid ECs
overflow / underflow	$\geq 1000.0 [a1]; < 0.0 [a2]$	
2 digit rounding		(,00x round up) [b1]; (,00x round down) [b2]
prefix		no '0' prefix [c1] exact '0' prefix [c2] exact '00' prefix [c3] exact '000' prefix [c4]
output suffix		'.yx' suffix ($x \neq 0$) [d1] .x0' suffix ($x \neq 0$) [d2] exact '.00' suffix [d3]

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- I used ‘set’ heuristics to divided the ‘prefixed 0’ ECs
- A range heuristics could be applied just as well
 - Condition
 - Whole part of decimal number x, let call it w
 - Intervals
 - w in [100..999] [b1]
 - w in [10..99] [b2]
 - w in [1..9] [b3]
 - w is [0] [b4]
- (Note: all these are VALID ECs)
- Will lead to the exact same test cases...



Computations

“Code without if’s”
... also requires some care



Computation Heuristics

- Computations have their own pitfalls: 0 and 1

If the specification of the unit under test defines an *arithmetic computation*, then

- **Addition and subtraction:** *If a computation includes addition or subtraction*, select one valid EC for the neutral element 0, and one valid EC for all other elements.
- **Multiplication and division:** *If a computation includes multiplication or division*, select one valid EC for the neutral element 1, and one valid EC for all other elements.

Example

- Specification:

```
// return a*x + b
public double linearFunction(double a, double x, double b) {
    return a*x + b;
}
```

- But: No conditions =>
 - Myers analysis will give only one test case =>
 - Could just be $a = x = b = 0$
- **Thus will not detect that the function below is wrong!**

```
// return a*x + b
public double linearFunction(double a, double x, double b) {
    return 0.0;
}
```

Example

- Specification:

```
// return a*x + b
public double linearFunction(double a, double x, double b) {
    return a*x + b;
}
```

If the specification of the unit under test defines an *arithmetic computation*, then

- **Addition and subtraction:** If a computation includes addition or subtraction, select one valid EC for the neutral element 0, and one valid EC for all other elements.
- **Multiplication and division:** If a computation includes multiplication or division, select one valid EC for the neutral element 1, and one valid EC for all other elements.

- Our computation heuristics thus leads to:

Condition	Invalid ECs	Valid ECs
multiplication ($a*x$)	-	$a = 1 [a1]; a \neq 1 [a2]$ $x = 1 [a3]; x \neq 1 [a4]$
addition ($+b$)	-	$b = 0 [b1]; b \neq 0 [b2]$

Note: the neutral element ECs need not be tested at all!

- Testcase: $a=7; x= 3; b=9 \Rightarrow \text{output} = 30$.

Computation Heuristics

- Example/Hint – *SigmaStone attacks with field support*

The resulting *attack strength* of a minion is the attack value of the minion itself, and to this value is added *field support*: +1 for each friendly fielded minion of the *same* class (and only them) up to a maximum of 4, and finally is added *boosts*

- +1 for every friendly minion of same class
 - Range $[0..4] + >= 5$
 - Implementation 1:
 - Value = attackStrength + sumOfFriendlyOfSameClass();
 - Implementation 2:
 - Value = attackStrength; // missed the summation here
- Picking 0 as representative element is problematic!



Boundary value analysis



Boundary value analysis

AARHUS UNIVERSITET

- Experience shows that test cases focusing on *boundary conditions* have high payoff.
- Some that spring into my mind are
 - *"off by one" errors in comparisons*
 - *if (x <= MAX_SIZE)* and not *if (x < MAX_SIZE)*
 - *null as value for a reference(pointer)*

Complements EP analysis

Definition: **Boundary value**

A boundary value is an element that lies right on or next to the edge of an equivalence class.

- Ex. Formatting has a strong boundary between EC [a1] and [a2]
 - 0.0 (-> '000.00') and -0.000001 (-> '------')
- It is thus very interesting to test $x=0.0$ as boundary.



Other Reliability Techniques

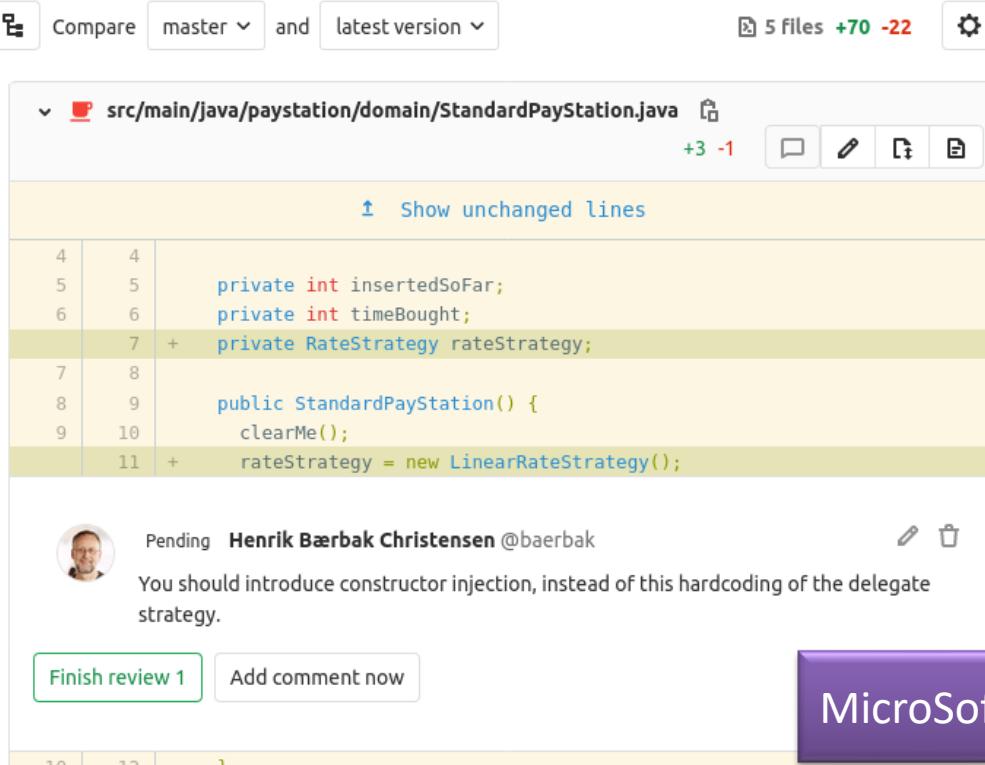
Testing is not the only way...

Systematic Review

- Systematic Review
 - A formalized, systematic, process of *people reading the code and identifying anomalies*
 - Pro:
 - Can find defects that no testing ever can
 - » Wrong comments
 - » Architectural flaws ('strategy is used incorrectly here')
 - Important learning
 - » Learn by reviewing the code of master coders
 - Con:
 - Manual/human/**slow/expensive**
 - Regression is too expensive
 - Bottleneck in releasing software

Systematic Review

- Supported by GitHub, etc



A screenshot of a GitHub pull request interface. The top bar shows 'Compare master and latest version', '5 files +70 -22', and a settings gear icon. The main area shows a diff of `src/main/java/paystation/domain/StandardPayStation.java`. The code has the following changes:

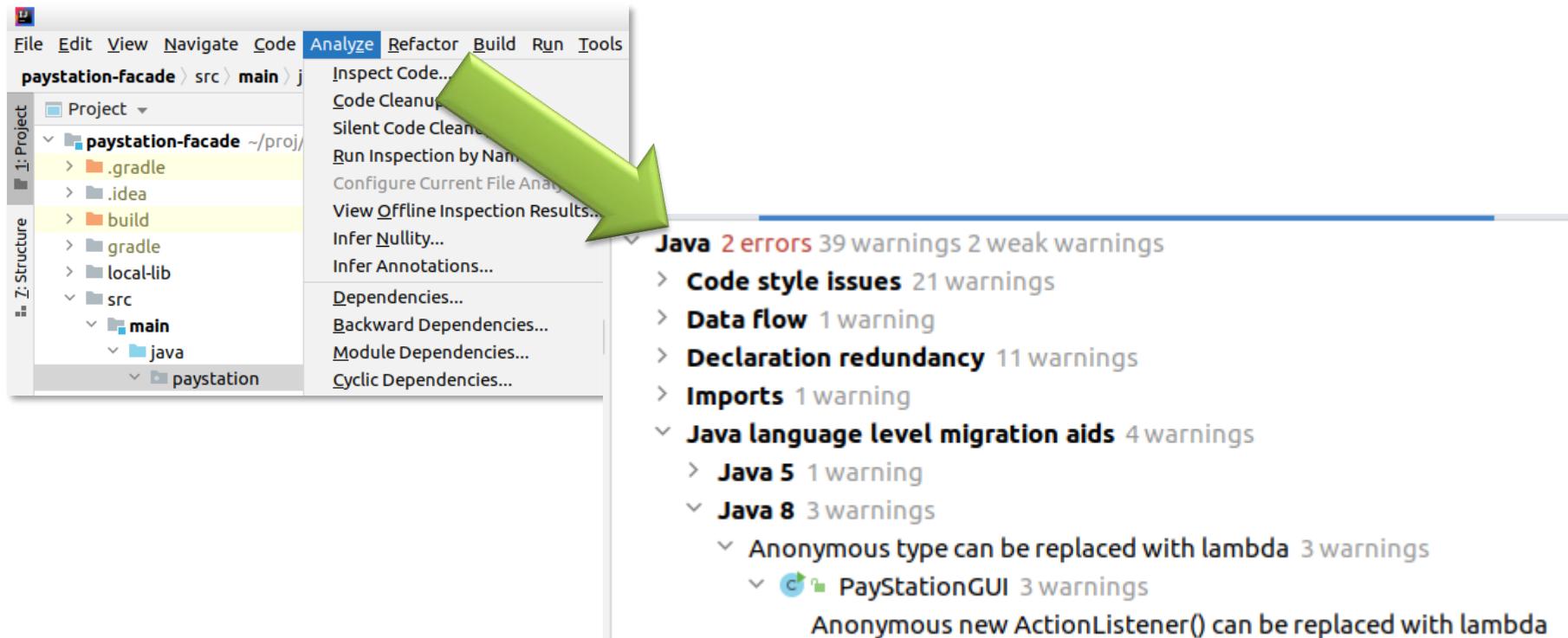
```
diff --git a/src/main/java/paystation/domain/StandardPayStation.java b/src/main/java/paystation/domain/StandardPayStation.java
index 1234567..8901234 100644
--- a/src/main/java/paystation/domain/StandardPayStation.java
+++ b/src/main/java/paystation/domain/StandardPayStation.java
@@ -4,5 +4,6 @@ private int insertedSoFar;
@@ -5,5 +5,6 @@ private int timeBought;
@@ -6,5 +6,7 @@ + private RateStrategy rateStrategy;
@@ -7,5 +8,6 @@ public StandardPayStation() {
@@ -8,5 +9,6 @@     clearMe();
@@ -9,5 +10,7 @@ +     rateStrategy = new LinearRateStrategy();
```

A comment from user **Pending Henrik Bærbak Christensen @baerbak** suggests: "You should introduce constructor injection, instead of this hardcoding of the delegate strategy." Below the code, there are buttons for "Finish review 1" and "Add comment now".

MicroSoft embraces review

Static Analysis

- Static Analysis
 - A review, but a **program** does it, using heuristics encoded



- Static Analysis
 - Pro
 - Fast and automated
 - Especially suited to find *security flaws*
 - Con
 - Restricted in the types of failures it can find
 - Primarily language level errors, not on architectural level
 - Overload of errors
 - I review many and find they are not errors but 'as I want it'
 - But they pop up every time I run the analysis => **error blindness**
 - » ***The one that I should have picked up drowns in all the information...***

- The biggest gun in the cupboard
- Mathematical proof that our algorithm is correct
- Much research (also here at CS), but so far (I think)
 - Techniques do not scale well
 - Math may be even harder to read than code
 - That is, the error may be in the proof!
 - Math is a model, often ignoring physical properties
 - No, the Stack is **not *infinite!*** No, memory is **not *infinite!*** Etc...



Discussion

A few key points

Key Point: Observe unit preconditions

Do not generate ECs and test cases for conditions that a unit specifically cannot or should not handle.

Key Point: Systematic testing assumes competent programmers

Equivalence partitioning and other testing techniques rely on honest and competent programmers that are using standard techniques.

Key Point: Do not use Myers combination heuristics blindly

Myers heuristics for generating test cases from valid and invalid ECs can lead to omitting important test cases.

- Equivalence Class Partitioning
 - EC = set of input elements where each one will show same defect as all others in the same set (representation)
 - Find ECs, use Myers to generate test cases.
- Boundary analysis
 - Be skeptical about values at the boundaries
 - Especially on the boundary between valid and invalid ECs